

Assignment 4: Kernels and SVM's

Submission: Tuesday May 12th
Maximum of 2 students per group

Prof. Fabio A. González
Machine Learning - 2009-I
Maestría en Ing. de Sistemas y Computación

1. Regression on strings

- (a) Implement a function that calculates a kernel over fixed-length strings,

$$k : \Sigma^d \times \Sigma^d \rightarrow \mathbb{R},$$

which counts the number of **coincidences** between two strings.

- (b) Implement the kernel ridge-regression (KRR) algorithm.
- (c) Use the KRR implementation and the kernel k to train a model using the training data set in <http://dis.unal.edu.co/~fgonza/courses/2008-I/ml/assign4-train.txt>. Evaluate the error of the model on the training data set. Plot the output of the model on the training data along with the real output values.
- (d) Evaluate the trained model on the test data set <http://dis.unal.edu.co/~fgonza/courses/2008-I/ml/assign4-test.txt>. Plot the results and discuss them.
- (e) Build a new kernel, k' , composing the kernel k with a polynomial kernel. Repeat steps (c) and (d).
2. Let $\mathbf{x} = \{x_1, \dots, x_n\}$ be a subset of a input data set X . Consider a kernel function $k : X \times X \rightarrow \mathbb{R}$, which induces a feature space $\phi(X)$:

- (a) Deduce an expression, that allows to calculate the average distance to the center of mass of the image of set \mathbf{x} in the feature space:

$$\frac{1}{n} \sum_{i=1}^n \|\phi(x_i) - \phi_S(\mathbf{x})\|_{\phi(X)},$$

where the center of mass is defined as

$$\phi_S(\mathbf{x}) = \frac{1}{n} \sum_{i=1}^n \phi(x_i).$$

- (b) Use previous expression to calculate the average distance to the center of mass of the following point set in \mathbb{R}^2 , $\mathbf{x} = \{(0, 1), (-1, 3), (2, 4), (3, -1), (-1, -2)\}$, in the feature spaces induced by the following kernels:
- $k(x, y) = \langle x, y \rangle$
 - $k(x, y) = \langle x, y \rangle^2$
 - $k(x, y) = (\langle x, y \rangle + 1)^5$

iv. Gaussian kernel

3. Controlling the model complexity

- (a) Download the Wisconsin Breast Cancer data set from [http://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+\(Diagnostic\)](http://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+(Diagnostic)) and divide it in a training set and a test set (50/50).
- (b) Train a SVM using a linear kernel. Find an optimal complexity parameter, C , plotting the training and test error vs. the complexity parameter. Use a logarithmic scale for C , $[2^{-5}, 2^{15}]$. Discuss the results.
- (c) Repeat item (b) using a Gaussian kernel.

4. Train an SVM for detecting whether a word belongs to English or Spanish:

- (a) Build a training and a test data sets. You can use the most frequent words in http://en.wiktionary.org/wiki/Wikt:Frequency_lists and http://es.wiktionary.org/wiki/Wikcionario:Palabras_m%C3%A1s_frecuentes_del_espa%C3%B1ol. Consider words at least 4 characters long and ignore accents.
- (b) Use an SVM software package that supports string kernels: LIBSVM, Shogun, etc.
- (c) Use cross validation to find an appropriate complexity parameter.
- (d) Evaluate the performance of the SVM in the test data set.